Rent-seeking elites, integration, and the coevolution of political institutions

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Abstract

This paper formally discusses the political consequences of international asset mobility. Within a given country, the elite can extract rents from the production sector. Factor mobility favors more efficient, and less extractive policies. This model yields several predictions. When masses are mobile, political inclusiveness spills over from abroad. Conversely, if the elite are mobile, but the masses are captive, political inclusiveness abroad favors polarization. In particular, liberal democracies provide an international framework in which patrimonial regimes thrive, and in which their own economic and political outcomes are negatively affected. Finally, tax evasion is shown to be a necessary outcome of asymmetric asset mobility. This entails both negative political consequences and little hope of reform.

1 Introduction

As history goes, capital mobility was key in the demise of absolute monarchies in Europe in the XVIIth and XVIIIth centuries, and the cornerstone of the advent of liberal democracies (Willard, 1934, as cited in Bates and Lien, 1985; North and Weingast, 1989). Often described as a “virtual senate”, an arm of large property against the arbitrariness of politics, global capital is implicitly assumed to rein in political elites, to constrain policies, and to promote institutions favorable to markets – transparency, impersonality, predictability, and the rule of law.

This swift description of history gives rise to a seeming paradox or difficulty: while the Parliament successfully claimed political power in seventeenth-century England, their counterparts in Latin America often failed in their similar endeavor.

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in the second half of the twentieth century, even though both were associated with increased capital mobility.

A key to solving that paradox seems to lie in a more careful sociological characterization of democratic movements in Europe and Latin America. Democratization in Europe was historically a conferral of political representation to an upper House, which mirrored the distribution of wealth in the society. Conversely in Latin America, a representative body would have been more democratic than plutocratic, in advance eliciting distrust from mobile capital owners, and encouraging these to seek informal ties with the governments rather than improved transparency or democracy. In both the European and the Latin American cases, increased capital mobility led to an improvement of market supporting institutions: lower taxes on capital, improved protection of property rights, and enforcement of contracts, but the parallel does not extend to political institutions. In fact, democratization happened only when representative bodies represented the interests of the owners of the more mobile asset, an argument present in Mahon (1996), and already hinted at in Bates and Lien (1985). Conversely, the concentration of wealth in Latin America favored regulatory capture, with legal reforms limited to those favoring incumbent firms and multinationals (central bank independence, free trade agreements, removal of capital controls) and a reinforcement of autocratic regimes thanks to informal ties between big property owners and the government (Boix, 2003).

This paper contributes to this analysis by making a novel assumption. Here, the decision makers are rent-seeking elite, who are able to divert a share of the tax revenue for their own benefit. This assumption is key, as it endogenizes the political dynamics of a country under the constraint imposed by capital mobility. The external constraint restricts the elite’s ability to capture rents (the state becomes less redistributive), and forces them to increase the provision of public goods (the state becomes more efficient). The elite are weakened, and the economic distortions associated with rent-seeking abate. Finally, inequalities diminish and output grows. The elite may even have to extend the franchise, understood as the ability for an increasing number of individuals to mobilize the capital, whether it be financial, social or cultural, to enter the elite.

This result is shown to be crucially dependent on the patterns of the cross-border mobility of assets. I explore an alternative scenario in which only the elite are mobile. The masses are captive: they cannot go work abroad, or their assets cannot be converted to another currency. The model then yields opposite results – that is, increased taxes, economic distortions and rent-seeking, and in the general case increased inequalities. Elite can increase the tax imposed on the masses while insulating their own wealth in the other country. They thus stabilize their ruling position, increase domestic taxes and economic distortions and reduce output. This scenario where the masses are captive can be interpreted from two
angles. First, it can provide a theoretical account of a society in which the elite and the masses hold different assets. Second, it provides a sociological account of who gets to influence the fiscal policy – this paper’s definition of elite.

The model provides several more predictions. First, liberal democracies may unwittingly contribute to reinforce the hold on power of rent-seeking elites, through the external framework they provide. When such elites can appropriate a share of tax revenue, and protect their ill-gotten wealth from domestic political hazard by investing in safe assets abroad, they are likely to implement more distortive, less efficient policies, and even possibly manage to prevent an extension of the franchise.

Second, since there are benefits for rent-seeking elite to ensuring the safety of their investments abroad, some resources are available to actively ensure that safety. Such elite may lobby the governments of liberal democracies. They may trade the safety of their assets abroad for international influence, for instance in the form of additional votes in multilateral institutions. Finally, they may even try to actively corrupt democratic officials into turning a blind eye on their politics, thanks to foreign party financing or bribes. This may in turn favor a more polarized outcome in liberal democracies.

Third, a small country in the position of establishing good enough institutions may seek to use this capacity to attract capital from abroad, thus becoming a tax haven. Actually, the elite of another country would never allow the assets owned by their masses to escape; but they may wish to evade the costs they themselves impose on these masses. The model has little to say on the politics of tax havens: the rent that the elite can extract on inflows is possibly large enough to dominate both local extraction and local efficiency considerations. If anything, this is consistent with the fact that small countries with various political regimes have in the past been described as tax havens. More interestingly, the political setup of this model predicts that a tax haven is a seemingly unavoidable companion of any big country dominated by an elite group.

Fourth, once they exist, tax havens may attract assets not only from liberal democracies, but also from patrimonial elite. In all cases, tax evasion has a distortive impact on policies as well as a polarizing political impact in the other country.

The following section examines the related literature. Section 3 develops the general framework of analysis, with a description of the productive sector, the political structure and the external constraint. Section 4 analyzes the political dynamics of a country with mobile masses, externally constrained and unconstrained. Section 5 considers a country with captive masses, also externally constrained and unconstrained. Several appendices are provided. The two first provide a formal model of the external constraint and derive its properties. The third one introduces public goods, shows and that the resulting framework is essentially
equivalent to the standard model, but justifies the interpretation of the taxes of the main model as *costs of doing business*. The last one introduces mineral rents.

## 2 Literature review

The model developed in this paper explores a variety of outcomes, in terms of economic distortions, inequalities, and rent-seeking. In these directions, however, its results are relatively straightforward, and a review of the related literature would be cumbersome. The outcome which is both less common and more interesting here is the political dynamics generated by the model. As many others, this paper assumes institutions are endogenous to development. For instance, Acemoglu and Robinson (2006c) focus on the economic determinants of regime change, in particular from elite control to democracy, and Acemoglu and Robinson (2006a, 2008) offer models of institutional persistence and change and the linkage from political to economic institutions.

In this paper, the state is controlled by self-interested agents who have the ability to capture some rents, as in Bates (1981); Levi (1989); Grossman and Noh (1994); Ades and Verdier (1996); La Ferrara and Bates (2001); Acemoglu (2003); Acemoglu et al. (2004); Acemoglu and Robinson (2006b), to name but a few key pieces of work in a prolific and far-reaching field. For critical reviews of this assumption see for instance Robinson (1998); Rodrik (2014).

The key contribution of this paper in this literature is to consider an open economy, and to formalize Mahon (1996)’s argument: when the owners of the mobile asset are not in the government, they extract an extension of the franchise; but when they have sufficient ties with the government, the dynamics may actually be reversed, with a strengthening of the elite in place. This provides a framework to discuss the coevolution of political institutions in integrated countries, which unifies several strands of the literature.

First, the “domino theory” is possibly the most influential model of political contagion of the second half of the twentieth century. In the more narrow perspective of this paper, the international diffusion of democracy has been documented only relatively recently (Huntington, 1991; Starr, 1991; Markoff, 1996; O’Loughlin et al., 1998; Whitehead, 2001; Gleditsch and Ward, 2006), though Leeson and Dean (2009) showed that the empirical diffusion effect is actually rather weak. The usual interpretation of this diffusion is a varying combination of several mechanisms, coercion, learning and emulation. Simmons et al. (2006) classify these mechanisms, and emphasize a fourth mechanism: competition between polities for the location of the productive assets. This paper provides what seems to be the first attempt at formalizing this argument, though arguably with a limited definition of democracy: it focuses on the inclusiveness of the political
process. This is only one aspect of democracy, admittedly far from the formal
definition of the term, yet possibly a key characteristic of actual democratic sys-
tems. To avoid any ambiguity, I will nevertheless refrain from using the term in
the core of the paper. The contingent prediction of this paper, positive democratic
spillovers in a country with mobile masses, and negative in a country where the
masses are captive, may account for this weaker-than-anticipated evidence.

Second, while Western liberal democracies, especially the United States and
the European Union, undeniably used their foreign policy to promote democra-
cies, evidence shows that they sometimes actively supported dictatorships (Robin-
son, 1996; Schmitz, 1999). This paper argues that liberal democracies may actu-
ally help buttress patrimonial regimes even when they do not interfere. Along
that line, a long tradition of economic thought, often dubbed as the school of
the “dependency theory”, has been describing the North-South divide as a self-
reinforcing pattern. This field of study never gained much traction in mainstream
economics, and for this reason any attempt at a short, yet encompassing review
of this literature is bound to be partial. Let me still take a shot at citing a few
key mechanisms that this literature uncovers. According to Perroux (1961, p. 61),
deredeveloped countries enter any exchange with developed countries at a dis-
advantage, a result of the military superiority, or monopsonistic position of the
latter. According to Frank (1967); Emmanuel (1969), international trade favors a
specialization of poorer countries in low value-added production traps. Cardoso
and Faletto (1979, p. 149) introduced a notion which is closer to this paper’s ar-
gument, when they described how international capital alters the patterns of class
relations in developing countries, eventually hijacking policies for other purposes
than development.

In the same line of arguments, a recent paper by Acemoglu et al. (2012) makes
a case for the asymmetric coevolution of the institutions of developed countries.
Their argument is that the comprehensive social welfare systems of certain coun-
tries (Scandinavia) favors the institutions of unbridled capitalism in others (the
United States). Generally, though, this issue of the coevolution of political insti-
tutions has received scant attention.

Third, this paper’s argument is that simply because they exist, liberal democrac-
cies offer a possible destination for capital flight. In small countries with poor
institutions, political and economic elite tend to allocate their assets abroad, while
implementing all the more extractive policies at home. In the case of Sub-Saharan
African, this is documented in Collier et al. (2004); Ndikumana and Boyce (2003,
2010, 2011), and in Ndikumana and Boyce (2012) in the case of Northern Africa.
The political impact of this capital flight has received a lot of media attention re-
cently, under the headline of “ill-gotten assets”. To my knowledge, however, it
has never received any formal treatment so far.

Fourth, the model predicts that the policies in small countries may be di-
verted towards attracting foreign capital, effectively turning such countries into tax havens. In line with the evidence in Dharmapala and Hines Jr. (2009), such policies generally translate into market-oriented institutions. Generally, however, while tax havens have received a lot of media attention too, data unavailability made their systematic documentation difficult, at least until Zucman (2013). He provides a detailed account of the process of capital flight from France into Switzerland, and a first sociological characterization of tax evaders, consistent with the model.

3 Economic determinants: the stage game

The game is adapted from Ades and Verdier (1996), who provide microfoundations for the political dynamics within one country. Their setup is here extended to an international framework.

3.1 The setup

The economy is composed of two countries, country A and country B (the competing jurisdiction). The latter will sometimes be referred to as “abroad”. The relative size of the population of country B is $n$.

Each individual in either country has one offspring and generations are altruistically linked by a “joy of giving” motive for bequests. Preferences are described by a common utility function $U(c_t, b_{t+1})$, where $c_t$ is consumption at time $t$ and $b_{t+1}$ the bequest left for a child born at time $t + 1$. $U$ is twice continuously differentiable, increasing in each argument $c_t$ and $b_{t+1}$, strictly concave and homothetic. The marginal rate of substitution $\frac{U'_c}{U'_b}$ between $c_t$ and $b_{t+1}$ is therefore an increasing function $\psi$ of $b_{t+1}$. Let $\rho = \psi^{-1}(1)$.

Individuals are each endowed with one unit of labor, which they can allocate to any of the two sectors in the national economy. They can also allocate it to the modern sector abroad, at a constant marginal cost $c$. The first sector has a decreasing returns to scale production technology. In this sector, $l$ units of labor produce $\phi(l)$ units of output, with $\phi' > 0, \phi'' < 0, \phi'(0) = \infty$ and $\phi'(1) = 0$. This activity accounts for an informal sector, not taxable, and can be thought of as a traditional/agriculture sector. Household production or underground sectors in many developing countries also fit the general characteristics described above. The other productive sector has a constant return to scale production function, and its technology is such that $l$ units of labor produce $l$ units of output. The activity is taxable, and can be thought of as the modern/manufacturing sector.

Taxation should not be interpreted here as the source of formal fiscal revenue
of the state (even though this is considered as an extension in appendix). In what follows, I will use the term \textit{tax} to speak of the rent extracted by the elite on the economy. This admittedly requires an extensive interpretation of the term (as well as of \textit{fiscal policy} and \textit{fiscal competition}), but this interpretation is straightforward from the point of view of the producer. As in Acemoglu (2006, p. 516), taxes should be understood as encompassing hidden costs, such as bribery and violations of property rights. Even the obligation made to foreign investors to take a local business partner and unexpected currency depreciations could be argued to qualify as additional forms of hidden costs; however such practices tend to create an asymmetry between domestic and foreign investors, which is beyond the purpose of this paper.

Individuals are endowed with a bequest $b_t$ left over by their parents in period $t - 1$. This bequest can be consumed, or it can be used to enter into political activity. If an individual decides to enter politics at time $t$, he will belong to the ruling elite. This enables him to decide on the level of taxes $\tau$ in the economy and to get a share of those tax revenues, unlike those who remain in the masses. If a individual decides to enter the ruling elite, he has to bear a fixed cost $\pi$ which may be country specific. Because of capital market imperfections, agents are not able to enter the elite using their future income as collateral. Thus, in order to belong to the elite at time $t$, an agent must have a starting level of wealth $b_t \geq \pi$.

Each agent’s life can be divided into four stages. The outcome of former stages is assumed to be common knowledge for all agents. In the first stage, (i) they receive their endowments, discover the external environment, and (ii) decide whether they will enter politics in stage 2. Let $z$ be the fraction of individuals who do not enter politics. Therefore, $1 - z$ will be the fraction of agents who belong to the elite: it is also a measure of the \textit{inclusiveness} of the political regime.

In stage 2, (iii) those individuals that have decided to enter politics vote for a proportional tax rate $T$ which would apply to the domestic formal sector if they manage to attract foreign capital. In doing so, they consider the reaction of other agents, both nationals and foreigners, and take into account the external environment.

In stage 3, (iv) the same individuals vote for a proportional tax rate $\tau$ which would apply to the domestic formal sector if they do not manage to attract foreign capital. Again, they consider the reaction of other agents, both nationals and foreigners, as well as the external environment. Stages 2 and 3 set a nonstandard framework, which I discuss extensively in the next section.

In the final stage, (v) the masses and the elite allocate their labor among the two national productive activities and possibly abroad, (vi) they produce and consume, and (vii) each agent decides how much bequest he will leave to his descendant.

The timing of events is as indicated in Fig. n°1.
Figure 1: The timing of one period

3.2 A critical discussion of the assumptions

The model is naturally recursive, yet the dynamics will be solved in continuous time, to avoid unrealistic mathematical complications. The economic activity other than inheritance – investment, production, consumption and bequests – happens at once. The state variable of the dynamic system is the initial distribution of bequests in both economies. Other than that, an equilibrium is reached in each period, which facilitates switching attention from the continuous dynamics of the economy to the recursive dynamics of a lineage. As it is, the problem still needs simplifying to become tractable.

One simplifying assumption is resorting to a warm glow motive for the inter-generational transmission of wealth. Implicitly, this assumes impure altruism or myopia on the part of ascendants towards their progeny (Andreoni, 1989). Pure altruism would suppose that ascendants use the bequests not as an end, but as a means to help their offspring achieve a higher level of well-being. Recent works, such as Harbaugh et al. (2007) for instance, show that human behavior is best described as a mix of pure altruism and warm glow. However, the possible discontinuity between the welfare of an individual entering the elite and that of a member of the masses introduces such complexity as to make the model intractable.

As a result of that assumption, and thanks to the homotheticity of preferences, the indirect utility of every individual, including the elites, is an increasing function of income. Actually, it is isomorphic to the sum of the income and the bequest:

\[ V_t = V(k(\rho)(B_t + R_t + b_t)) \]  

where \( k(\rho) \) is a constant which depends only on \( \rho \), \( V \) is an increasing function,
and $R_t$ are the rents collected from political participation. $R_t$ is zero if an agent does not belong to the elite. If an agent participates in politics, he shares equally the rents collected with other members of the elite. Thus, for an agent who participates in politics, $R = \frac{tl}{1-z} - \pi$. This assumption, of homothetic preferences, is not significant. Its only purpose is to yield explicit solutions.

A second key assumption is the choice of the fiscal decision making process. There would theoretically be three possible sources of tax revenues. The elite could possibly tax bequests, the national income (“residence-based” taxation), the domestic income (“source-based” taxation), or use various forms of non-distortionary, lump-sum taxation. I focus here on domestic income as the main source of taxation, for three reasons. First, the compliance costs involved in taxing income on assets invested abroad is disproportionately higher than in taxing domestic income (Blumenthal and Slemrod, 1995; Gordon and MacKie-Mason, 1995; Gordon and Bovenberg, 1996). Second, bequests are arguably in the form of financial or social capital, both much harder to capture than the physical capital involved in the production process. Third, lump-sum taxation would effectively make tax competition inoperative, and in practice (head taxes for instance) is both inapplicable and inequitable; identically, Bucovetsky and Wilson (1991) shows that if countries are able to tax based on both residence and source, they are also able to make tax competition inoperative.

Even keeping only domestic income as a source of fiscal, revenue, in the most general formulation, $T$ and $\tau$ should be expressed as functions of the amounts of assets effectively supplied by the various groups. Since the aim of this work is to study the interaction of two economies, it is reasonable to still reduce the dimensions of the space of possible fiscal decisions. The formulation chosen provides such a simple and intuitive fiscal framework.

Individuals can allocate their asset in the domestic formal sector, and be taxed by the local authority. The foreign formal sector offers them the outside option of being taxed in another jurisdiction. When allocating their asset abroad, agents incur an additional marginal cost $c \in [0, 1]$, which accounts for language barriers, network effects (and even asymmetries of information, as in Gordon and Bovenberg, 1996, but information issues fall outside the scope of this paper) etc. $l$ units of asset allocated to the domestic formal sector generate $(1 - \tau)l$ units of after-tax income, while they would generate $(1 - c)(1 - T^B)l$ if in the formal sector abroad. For simplicity, I assume that all things equal, an agent prefers to invest domestically, so if the domestic and the external returns on the asset are equal, then agents allocate their asset domestically. Because of constant returns, the asset of one agent is therefore allocated in full to the formal sector of only one jurisdiction. Finally, if agents invest $l$ in either formal sector, they invest the remainder $1 - l$ in the traditional sector, which generate $\phi(1 - l)$ units of income. The purpose of introducing the informal sector is to allow individuals to substitute away from the
taxed activity. Only if the supply of assets is elastic can taxes have distortionary effects, an essential feature of the model. Let me write the economic income of an individual $B = (1 - \tau)l + \phi(1 - l)$ or $B = (1 - c)(1 - T^B)l + \phi(1 - l)$, depending on the case.

Letting the masses of a country allocate their asset to the other country is always a dominated solution from the point of view of the elite of the former country. Indeed, facing an external environment characterized by $T^B$ and $c$, the elite can set $\tau = 1 - (1 - c)(1 - T^B)$. This would make sure all agents would derive the same economic economic income whether they allocate their asset domestically or abroad. As a result, they would all invest domestically, and the elite would then derive a political rent $\frac{\tau}{1 - \tau}$ on top of their identical economic income. In other words, in equilibrium, the masses never allocate their assets abroad. No level of $T^B$ would allow either elite of country $B$ to actually attract the assets owned by the masses of country $A$. Thus, the modern sector abroad accounts for the relevant external environment of the country. This simplification is the result of the nonstandard framework set by stages 2 and 3 in Fig. n°1. In the two-stage game of fiscal competition I propose, stage 2 establishes the external constraint on the other country’s fiscal policy. In stage 3, the elites decides on the effective costs of doing business under this external constraint.

Since the asset is supplied by each individual in full to one country, groups are homogeneous, and masses never allocate their assets abroad, four possible situations arise. Assets may actually not cross the border at all; elite of either country may allocate their assets abroad while the masses keep it at home; finally, elite in both countries may allocate their asset in the other country. The equilibrium described in the last situation is counter intuitive, and it is not robust to a number of possible mechanisms: it can therefore be neglected. Overall, this simplification still offers a reasonably rich framework.

Finally, one last assumption should be made explicit. I assume that the same tax rate $T$ applies to the domestic production, whether it be owned by national or by foreign investors, by members of the masses and elite. This assumption is not straightforward. It can admittedly be very difficult to establish the identity (and nationality) of the ultimate beneficiary of an investment, as as anti-money laundering authorities know very well. Empirically, there are various forms of treaties which involve a legal arrangement to rule out such discrimination: agreements between sovereign parties, such as bilateral tax and investment treaties (Elkins et al., 2006), between a sovereign and a private party, such as establishment agreements, and even multilateral agreements, as exemplified by art. 65 of the Treaty on the Functioning of the European Union. Nevertheless, Janeba and Peters (1999) show if the states can discriminate between national and foreign investors, they theoretically do so in the general non-cooperative equilibrium. Does it affect the results of the model? In the framework at hand, the fiscal decision directly reflects the
trade-off between the extractive and the efficiency motives of the elite. If the elite are able to dodge the tax, the efficiency motive disappears, and the elite would consistently maximize extraction from the rest of the economy. If they were able to fully discriminate between domestic and foreign ownership, the tax rate of the other country is consistently capped by the cost of moving one’s assets abroad. Overall, this no-discrimination assumption should not be interpreted too literally, but still seems to be a reasonable simplification.

3.3 Labor supply

In stage 4, consumers decide how to allocate their labor and how much bequest to leave to maximize their utility, depending on the tax rate $\tau_t$ they face:

$$\max_{l_t, b_{t+1}} U_t = U(c_t, b_{t+1})$$

s.t. $c_t + b_{t+1} = (1 - \tau_t)l_t + \phi(1 - l_t) + R_t + b_t$.

Whether for a member of the elite or of the masses, the first order condition can be written:

$$1 - \tau_t = \phi'(1 - l_t)$$  \hspace{1cm} (2)

which defines an optimal labor supply $l_t = l(\tau_t) = 1 - (\phi')^{-1}(1 - \tau_t)$, with $l$ a decreasing function of the level of taxation, $0 < l(0) < 1$ and $l(1) = 0$. Thanks to the homotheticity of preferences, consumption and bequests are given by:

$$\begin{cases} 
  c_t = \frac{1}{1+\rho} (B_t + R_t + b_t) \\
  b_{t+1} = \frac{\rho}{1+\rho} (B_t + R_t + b_t) .
\end{cases}$$  \hspace{1cm} (3)

Both consumption and the level of bequests left over for the generation born at time $t + 1$ are a fixed proportion of the disposable income $B_t + R_t$, where $B_t = (1 - \tau_t)l(\tau_t) + \phi(1 - l(\tau_t))$. Notice that if agents allocated their asset abroad, their decision to supply labor is based on an “apparent” tax rate of $1 - (1 - c)(1 - \tau^E_t)$.

3.4 Tax policy

In stage 3, the elite choose $\tau_t$ to maximize their utility. If the fiscal policy is not externally constrained, this yields the following first order condition:

$$z_t l(\tau_t) + \tau_t l'(\tau_t) = 0$$  \hspace{1cm} (4)

which defines implicitly an optimal autarkic tax rate $\tau_t = \tau(z_t)$. For a well defined concave problem, eg. when
∀z, l''(τ(z)) < \frac{(z + 1)l'(τ(z))}{τ(z)}, \quad (C1)

then τ is increasing in z, the share of the total population that does not participate in politics. The elite sets τ_i taking into account two effects. The first effect, characterized by the first term of the previous expression, is the marginal revenue extraction, while the second effect, described by the second term, negative, is the distortion of the elite member’s labor allocation associated with taxation. When z_i is close to 0, and the elite comprises the whole population, there is no revenue extraction. When z_i is close to 1, the revenue extraction effect dominates. The revenue extracted displays the property of a Laffer curve, and there is therefore a value \bar{τ} = \arg \max τl(τ) which maximizes the revenue extraction. As a consequence, τ' > 0, τ(0) = 0 and τ(1) = \bar{τ}.

For now, let me assume that the masses are mobile internationally: they can possibly allocate their asset abroad. The elite therefore set the tax rate so as to retain their asset, eg. by setting τ_i ≤ 1 − (1 − c)(1 − T_B^i). Effectively the external environment constrains the fiscal policy in the country. To summarize, the optimal tax rate actually implemented can be written:

\[ τ_i = \min \left[ τ(z_i), 1 − (1 − c) \left( 1 − T_B^i \right) \right] \quad (5) \]

Let me take a step back and discuss the external constraint and the determinants of T_B^i. In the chosen framework, no level of T_B^i would allow either elite to actually attract foreign assets. A Nash equilibrium of the game never actually involves any asset flow between the two countries. The concept unfortunately leads us no further: in terms of best response the elite of the other country is indifferent between any level of T_B^i. However, the rate which maximizes

\[ B(T_B^i) + \frac{T_B^i(nl(T_B^i) + l(1 − (1 − c)(1 − T_B^i)))}{n(1 − z_B)} \]

implicitly defines a tax rate T_B^i = T(\bar{z}_B, \frac{1}{n}) as a function of z_B (the share of the masses of the second country) and n, increasing in z_B.1 A higher T_B^i means relaxing the external constraint on the tax policy. While the relative size of the

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1This rate can be distinguished as the unique strategy yielding an extensive-form trembling hand perfect equilibrium. In appendix, I show that the game is also weak-dominance solvable, and that this rate can be derived as the unique equilibrium of a process of iterated elimination of weakly-dominated strategies. Moreover, the two concepts are robust to alternative specifications of the game. The only important assumption is that the first country be able to make the last move in setting the tax rate, which adequately accounts for a fiscal policy under an external constraint. T_B^i therefore appears like the “natural” rate to describe the external environment that the first country faces at the beginning of stage 1, resulting in the most reasonable equilibrium among all possible Nash equilibria.
two countries has an ambiguous effect on this constraint, the size of the elite has an unambiguous effect. As for \( \tau_t \), \( T_t^B \) reflects the inclusiveness of the political process in the competing jurisdiction. Presumably, an inclusive jurisdiction sets up an external framework characterized by a low \( T_t^B \), while a narrow elite would be associated with a higher \( T_t^B \): an inclusive elite abroad exacerbates the external constraint on the elite at home. In other words, it is easy to provide a formal model of \( T_t^B = T(z_t^B, I_t) \), where \( I_t \) the amount of asset inflows this elite is trying to attract, and where \( T \) is an increasing function of \( z_t^B \).

Finally, \( c \), the cost of the mobility of asset, deserves a small discussion. The higher \( c \), the less stringent the external constraint. A policy affecting \( c \) would therefore allow the policymaker (the domestic elite or an international institution) to affect the impact of the external constraint on its policy. Here, it is implicitly assumed that \( c \) is exogenously determined, by the language barrier, external regulations, networks effects etc. In real life, however, Wong (2008) discusses the extent to which the elite have some degree of control over the capital controls and use those to affect their own chance of staying in power.

### 3.5 Size of the elite

In stage 1, individuals decide to enter the elite or remain in the masses. Two conditions determine this decision. The first is that \( b_t \geq \pi \): the agent must not be liquidity constrained. He must be able to pay the entry cost into the elite. The second condition is that it is profitable to enter, ie \( R_t \geq \pi \). The former condition involves no consideration of other individuals, the latter on the contrary depends on the decision of other individuals: if enough individuals are able to pay \( \pi \) (liquidity constraint not binding), entry may drive political rents to zero.

Let me take a closer look at the latter condition, with \( R_t = R(z_t) = \frac{\tau(z_t)(T_t^B)}{1-z_t} \) when the fiscal policy is not externally constrained. \( R \) increases in \( z_t \), \( R(0) = 0 \), and \( R(1) = \infty \): as long as the fiscal policy is unconstrained, there exists a unique \( \overline{z} \) such that \( R(\overline{z}) = \pi \). By analogy, when the fiscal policy is externally constrained, \( R_t = R(z_t, T_t^B) \). Since \( 1 - (1 - c)(1 - T_t^B) < \tau(z_t) < \tilde{\tau} \), agents are on the left-hand side of the Laffer curve: \( R \) is an increasing function of both \( T_t^B \) and \( z_t \). \( R(\overline{z}, 1 - (1 - c)(1 - T_t^B)) = \pi \) therefore defines \( \overline{z} \) as a decreasing function of \( T_t^B \); it takes fewer elite members to exhaust the political rents. In other words, the profitability condition is unlikely to be binding when the external constraint is not binding or weak (exclusive jurisdiction abroad), but becomes much more present when the external constraint is strong (inclusive jurisdiction abroad). Possibly, if \( c \) is high enough and \( \pi \) low enough, \( \overline{z} \) is constant (low) throughout.

At any time \( t \), we can then define the share of the total population that is liquidity constrained, given by \( q_t = F_t(\pi) \), where \( F_t \) is the cumulative distribution function of bequests at time \( t \). Thus, \( F_t(\pi) \) shows the fraction of people that have
received a bequest less than \( \pi \) at time \( t \). To summarize, \( z_t \), the fraction of the population that belongs to the masses, is given by:

\[
z_t = \max[q_t, \bar{z}].
\]  

(6)

4 Political evolution

4.1 The dynastic evolution of bequests

The total after tax income of the masses is \( B_t = B(z_t, T_B^t) = (1 - \tau_t)l(\tau_t) + \phi(1 - l(\tau_t)) \), where \( \tau_t = \min \left[ \tau(z_t), 1 - (1 - c)(1 - T_B^t) \right] \). By analogy, let me define the total after tax income of the elite, net of political participation cost: \( A_t = A(z_t, T_B^t) = B_t + \frac{\tau_t l(\tau)}{1 - z_t} - \pi \). To simplify notations, I will simply use univariate income functions \( A(z) \) and \( B(z) \) when the fiscal policy is unconstrained.

When the profitability constraint is binding (and not the liquidity constraint), political rents are driven down to zero, and the income of the elite and of the masses is the same: \( \forall T, A(\bar{z}, T) = B(\bar{z}, T) \). If the liquidity constraint is, \( A > B \). Thereafter, I will only study the case where it is the liquidity constraint which matters for political participation.

When the external constraint is not binding, \( A \) and \( B \) are respectively increasing and decreasing in \( z \):

\[
\begin{align*}
\frac{dA}{dz} &= \frac{\tau l}{(1 - z)^2} > 0 \\
\frac{dB}{dz} &= -l\tau' < 0
\end{align*}
\]

and when it is:\(^2\)

\[
\begin{align*}
\frac{\partial A}{\partial z} &= \frac{\tau l}{(1 - z)^2} > 0 \\
\frac{\partial A}{\partial T} &= \frac{1 - c}{1 - z}(zl + \tau l') > 0 \\
\frac{\partial B}{\partial z} &= 0 \\
\frac{\partial B}{\partial T} &= -(1 - c)l < 0.
\end{align*}
\]

When the fiscal policy is not externally constrained, a narrower elite imposes a higher tax rate. Constrained or not, a higher tax rate implies a lower income for the masses, and a higher income for the elite. When it is constrained, the size of the elite does not affect the income of the masses anymore, but it does affect how widely the political rents must be distributed: again, the narrower the elite, the higher income for each elite member.

The bequests left at time \( t \) by agents that belong respectively to the elite and to the masses are given by:

\(^2\)By definition of the function \( \tau \), \( zl(\tau) + \tau l^\prime(\tau) > 0 \) for any \( \tau < \tau(z) \), which is the case when \( \tau = 1 - (1 - c)(1 - T_B) \). This proves that the partial derivative of \( A \) with respect to \( T \) is positive. All other derivatives are straightforward.
These two equations describe the dynamics of wealth accumulation for both
the elite and the masses, as a function of the level of participation in both countries.
They are represented in Fig. n°2.

\[
\begin{align*}
    b_{t+1} &= \frac{\rho}{1+\rho}(A_t + b_t) \quad \text{and} \\
    b_{t+1} &= \frac{\rho}{1+\rho}(B_t + b_t).
\end{align*}
\]  

(7)

4.2 Elite dynamics

Either \( q_t \geq z_t \), and the liquidity constraint remains binding: individuals such that
\( b_t \geq \pi \) can pay the sunk cost necessary to being in the elite, and \( z_t = q_t = F_t(\pi) \);
or \( q_t < z_t \), and the binding constraint is the profitability constraint. In that case
individuals with sufficient bequests are indifferent between being members of the
elite and of the masses in equilibrium. Along with Eq. n°6, Eq. n°7 characterizes
the whole dynamics of the system. Let me describe the dynamics of \( q_t \) from \( t \) to
\( t + 1 \).

If \( \rho A_t < \pi \) (case illustrated by Fig. n°3), then individuals that inherited a
bequest \( b_t \in [\pi, \frac{1+\rho}{\rho} \pi - A_t] \) can pay the cost of entering the elite, but they do not
provide a sufficient bequest \( b_{t+1} \) to their children for them to pay the cost at time
\( t + 1 \). Individuals such that \( b_t < \pi \) are members of the masses. They leave a
bequest \( b_{t+1} = \frac{\rho}{1+\rho}(B_t + b_t) < \frac{\rho}{1+\rho}(A_t + \pi) < \pi \), so their children remain in
the masses. From any such \( t \) to \( t + 1 \), \( q \) and the size of the elite are therefore non-
increasing, and in a dynasty of elite members, the bequest left to the successors
decreases. Finally, if the liquidity constraint is binding at $t$, it remains binding at $t + 1$.

![Figure 3: High $\pi$ when the liquidity constraint binds.](image)

If $\rho B_t \leq \pi \leq \rho A_t$ ($B_t < A_t$ can only happen if the liquidity constraint is the binding constraint, so $z_t = q_t$), then individuals that inherited a bequest $b_t \geq \pi$ are members of the elite (case illustrated by Fig. n°4). They provide a bequest $b_{t+1} = \frac{\rho}{1+\rho} (A_t + b_t) > \pi$ to their children, who can remain in the elite. Individuals that inherited a bequest $b_t < \pi$ are members of the masses. They provide a bequest $b_{t+1} = \frac{\rho}{1+\rho} (B_t + b_t) < \pi$ to their children, so these remain in the masses. From any such $t$ to $t + 1$, the size of the elite is unaffected. In any dynasty, the bequest left to successors moves closer to $\rho B_t$ for a member of the masses, and to $\rho A_t$ for a member of the elite. The liquidity constraint remains binding in period $t + 1$.

And finally, if $\pi < \rho B_t$ (case illustrated by Fig. n°5), then individuals that inherited a bequest $b_t \in \left[\frac{1+\rho}{\rho} \pi - B_t, \pi\right]$ cannot pay the cost of entering the elite, but they provide a bequest to their children which allows them to pay the cost at time $t + 1$. Individuals who can pay the cost of entering the elite leave a bequest which also allows their children to pay the cost at time $t + 1$. From any such $t$ to $t + 1$, $q$ and the size of the elite are therefore non-decreasing. In a dynasty of individuals who cannot pay the cost of entering the elite, the bequest left to the successors increases; as a consequence, if the liquidity constraint is binding, the bequest left in a dynasty of members of the masses increases. Finally, if the profitability constraint is binding at $t$, it remains binding at $t + 1$, and the number of persons in the elite remains constant.
4.3 Dynamics and equilibria in a closed economy

To better understand the dynamics of the previous section, let me now examine the equilibrium towards which the country converges. As a first step, let me consider the case where the tax policy is unconstrained, and remains thus throughout: going through this exercise simplifies the exposition. One additional assumption makes the exposition considerably simpler at no loss of generality. Let the initial distribution be described by a continuous and positive density function \( f_t \) and an associated cumulative function \( F_t \) on a closed interval \([b_t^-, b_t^+]\) with \( 0 \leq b_t^- \) small enough and \( \pi < b_t^+ \). The previous considerations yield three possible initial situations.
First, when $\rho A_t < \pi$, the number $q$ of individuals who can pay the cost $\pi$ of entering the elite decreases between time $t$ and $t+1$ (cf. Fig. n°3). In other words $q_{t+1} < q_t$. The sequence $q_t$ is bound upward by 1, so it converges toward a limit. That limit cannot be lower than $\bar{z}$.\(^3\) In other words the profitability constraint cannot remain binding forever in that scenario. When the liquidity constraint is binding, $z_t = q_t$ is an increasing sequence, and so is $A_t = A(z_t)$. There exists a finite time $S > 0$ such that $\rho A_S < \pi \leq \rho A_{S+1}$.\(^4\)

When $\rho B_t \leq \pi \leq \rho A_t$, which can be the initial situation or the outcome of the previous situations, there is no social mobility in the economy (cf. Fig. n°4).

Lastly, when $\pi < \rho B_t$, the number $q$ of individuals who can pay the cost $\pi$ of entering the elite increases between time $t$ and $t+1$ (cf. Fig. n°5). In other words $q_{t+1} < q_t$. The sequence $q_t$ is bound downward by 0, so it converges toward a limit. One more time, that limit cannot be higher than $\bar{z}$.\(^5\) In other words the liquidity constraint cannot remain binding forever in that scenario. When the profitability constraint is binding, $q_t$ is decreasing and converges towards 0. The group of people able to apply for elite status grows until it encompasses the whole population, but in equilibrium, individuals of that group are indifferent between becoming elite or remaining in the masses, and do no better than individuals who remain liquidity constrained. To sum up:

**Proposition 1** When $\rho A_t < \pi$, the elite shrinks until in a finite time $S_h \rho B_{t+S_h} < \pi \leq \rho A_{t+S_h}$.

When $\rho B_t \leq \pi \leq \rho A_t$, the size of the elite remains constant and the wealth distribution converges towards the degenerate distribution $\rho B_t$ with mass $F_t(\pi)$ and $\rho A_t$ with mass $1 - F_t(\pi)$.

Finally when $\pi < \rho B_t$, the elite expands until in a finite time $S_l$ its size reaches $1 - \bar{z}$, and the wealth distribution converges towards the degenerate distribution $\rho A(\bar{z}) = \rho B(\bar{z})$ with mass 1.

Prop. n°1 yields two possible equilibrium outcomes: a polarized society whenever $\rho B_t \leq \pi$ and an inclusive one otherwise. When $\pi$ is high, the elite first shrinks, which allow its members to increase taxes and political rents, at the

\(^3\)The proof is by contradiction. $A$ is a function of $z$ only, which is stable equal to $\bar{z}$ when the profitability constraint is binding. In that case $q_{t+s} = F_{t+s}(\pi) = F_{t+s-1}(\frac{1+s\rho}{\rho} \pi - A) = F_t(\frac{1+s\rho}{\rho} \pi - \rho A(1 - \frac{1+s\rho}{\rho} \bar{z}))$ which converges to 1. Therefore there exists an $s$ for which $q_{t+s} > \bar{z}$, a point at which the liquidity constraint becomes binding.

\(^4\)The proof is again by contradiction. Suppose for all $t > 0$ we had $\rho A_t < \pi$. Since $z_t$ is increasing and bounded, it must converge. $A$ tends to $\infty$ when $z$ tends to 1, so since $A_t$ is bounded, by continuity, the limit of $z_t$ must be lower than 1. That means the dynasty with the largest endowment should forever stay in the elite. An argument similar to the previous proof shows this is impossible.

\(^5\)The proof can be replicated from the previous one.
cost of some economic efficiency and increased inequalities, before it stabilizes. When \( \pi \) is intermediate, taxes, distortions, economic incomes and political rents are stable, and wealth converges in both social groups towards their respective equilibrium level. For convenience, let me call \( \tilde{z}_t \) the size of the elite when it has stabilized (at \( t + S \) in the first case, and \( t \) in the second), starting from the distribution \( F_t \). This outcome corresponds to the polarized society. When \( \pi \) is low, the elite expands until political rents are driven down to zero. Taxes end up covering only the cost of entering the elite. From that point on, a process of social and political equalization takes place. The political dynamics in a closed economy can be summarized as on Fig. n°6.

4.4 Two-country dynamics

Let me now consider two countries in interaction. The distribution of wealth now evolves jointly in two countries. For the purpose of the exposition, let me assume that country \( A \) is initially constrained by the fiscal policy of country \( B \). The external constraint affects the incomes of the elite and of the masses. The income of the elite is lower than it would be in autarky, and the income of the masses is higher. It is useful to distinguish two channels through which the incomes evolve in a constrained country. First, the size of the national elite may change, which affects how widely the tax proceeds have to be distributed, and therefore the income of the elite. Second, the tax rate may be at least momentarily determined by the external constraint, and therefore by the inclusiveness of the competing jurisdiction. The technical framework is now well established, and many details can therefore be spared, in particular with respect to the profitability constraint. Three states arise, for the same ranges of parameters as for the closed economy.

When \( \rho A_t < \pi \) (first state, high cost of entering the elite), the elite shrinks, and would ideally like to increase taxes and distortions as it does. The external constraint might make that impossible. As before, a shrinking elite means a higher share of the political rent for each remaining elite member. Now, however, the tax rate reflects the political evolution in country \( B \). If country \( B \) is growing more inclusive, \( T_t^B \) decreases. It may decrease fast enough for the tax rate channel to dominate the shrinking elite channel: the income of the elite may decrease.
This is a temporary situation at best, however: the shrinking elite effect eventually dominates when the elite is small enough. Whatever happens in country $B$, there exists a finite time $S'$ such that $\rho A_{S'} < \pi < \rho A_{S'+1}$: the closed economy results holds. The constraint on the fiscal policy may become slack only if the elite in $B$ is shrinking fast enough. While it remains binding, the taxes are lower, the income of the masses is higher, inequalities are unequivocally lower, and the elite shrinks further than in a closed economy: both the dynamics and the equilibrium are altered because of the external constraint.

When $\rho B_t \leq \pi \leq \rho A_t$ (second state, intermediate cost of entering the elite), the elite remains stable. Only the tax rate channel remains. If the elite in $B$ becomes less inclusive, $T^B_t$ rises, which alleviates the external constraint on $A$’s fiscal policy. $A$’s elite may increase its domestic tax rate, to its own benefit and to the detriment of the masses. As a consequence, the elite remains stable throughout. If the elite in $B$ is stable, or stabilizes at a level where $\tau(z^A) > 1 - (1 - c)(1 - T(z^B, \frac{1}{n}))$ still, then taxes, distortions, political rents, and inequalities are lower than they would be in autarky. If the elite in $B$ expands, the external constraint is exacerbated. The elite in $A$ is forced to lower its tax rate in the process. The income of the masses increases, and that of the elite decreases. As long as $\rho B_t \leq \pi \leq \rho A_t$, the heirs of elite members remain in the elite, and the children of the masses remain in the masses. If at some point the income of the elite decreases below $\frac{\pi}{\rho}$ (eg. if at some point $\rho A(z_t, T^B_t) < \pi$), the previous considerations apply: the elite temporarily shrinks, before it stabilizes again. Conversely, if at some point the income of the masses increases above $\frac{\pi}{\rho}$ (eg. if at some point $\pi < \rho B(z_t, T^B_t)$), some members of the masses are able to switch to the elite. In that case, an expanding elite can only result in the liquidity constraint not being binding at some point. The size of the elite is $z_t = \bar{z}$ thereafter, there are no political rents anymore, and the whole population converges to a state of perfect equality.

When $\pi < \rho B_t$ (third state, low cost of entering the elite), the elite becomes more inclusive. While the tax rate $\tau(z_t)$ it would set if unconstrained decreases, the actual tax rate $\tau_t < \tau(z_t)$ is determined by the external constraint. If the elite in $B$ shrinks fast enough, $T^B_t$ increases, and the tax rate channel may possibly dominate the expanding elite channel, thus actually reducing the income of the masses; if their income decreases below $\frac{\pi}{\rho}$, the elite stabilizes. Obviously, this is not possible if the elite had not been in a position to stabilize itself in a closed economy: this extreme case simply corresponds to a temporary elite expansion under a fast dissipating constraint. Except in that specific case, whether or not the constraint is raised thanks to a decreasing $\tau(z_t)$, the elite becomes increasingly inclusive, even once the external constraint has become slack. The external constraint forces a lower tax rate $\tau_t = 1 - (1 - c)(1 - T^B_t)$. This accelerates the
convergence, with lower taxes, distortions, political rents and inequalities. During the convergence, $\tau(z_t)$ decreases and converges towards $\tau(\bar{z})$. If this is lower than $1 - (1 - c)(1 - T_B^T)$ after $T_B^T$ has stabilized, the external constraint becomes slack before the liquidity constraint, and everything proceeds as if the economy was closed. But even if it is higher, equilibrium political rents are still zero. This implies a narrower elite than in the closed economy inclusive equilibrium.

Meanwhile, in states 1 and 2, the elite dynamics in $B$ are more simple. Except in a relatively extreme scenario, $B$’s fiscal policy remains unconstrained, and the closed economy results apply. If the elite in $B$ shrinks enough (for instance if $\pi^B$ is very high), the constraint on $A$’s fiscal policy may become slack. In the extreme scenario, there may even be a point after which the fiscal policy of $A$ becomes constraining for the policy of $B$. Country $B$ would then find itself in first constrained state.

In state 3, in general, the elite of country $A$ becomes inclusive: the constraint on $A$’s fiscal policy therefore alleviates, until it eventually becomes slack. $A$’s fiscal policy may even end up constraining $B$’s, especially if, meanwhile, the elite in $B$ shrinks. Again, country $B$ would then find itself in the first constrained state. Even if the elite in $B$ is stable – or if it has stabilized after shrinking – the expanding elite in $A$ may put the fiscal policy of country $B$ under constraint. Country $B$ would then find itself in the situation described above in the second constrained state.

These considerations provide a full characterization of the coevolution of the political institutions of countries $A$ and $B$, in the form of an algorithm. As for a closed economy, there are only two possible equilibrium states for each country: polarized where $\rho_B \leq \pi \leq \rho_A$, or inclusive, where $\pi < \rho_B = \rho_A$. Additional complexity arises, in the dynamics towards these equilibria, but this complexity remains under control, thanks to two considerations. First, the size of the elite of each country plays the role of a state variable, and these state variables are always monotonous. Second, while there may be some loops between states 1 and 2, the number of such loops is finite. Even though theoretically and mathematically possible, any situation generating more than three switches between states in the dynamics towards the equilibrium for any given country is unlikely to arise.

### 4.5 Dynamics and equilibria in an open economy

Furthermore, a number of the possible paths generated by the two-country dynamics are unrealistic and unnecessarily complex. The constraint on a given country is not set by only one country, but by any other country with sufficient business opportunities and sufficiently low costs of doing business (taxes). A sudden increase of the costs of doing business in all possible competing jurisdiction is an unlikely scenario.
It is reasonable to simplify the previous exposition by considering a country which faces an stable external constraint, characterized by a fixed $T^B$. This external constraint can be thought to account for investment opportunities on the international market for capital. The concept of international capital market becomes very intuitive: the standard it sets is the marginal available investment opportunity for a mobile capital owner. The dynamics of country $A$ under this constraint are considerably simpler, and it becomes reasonable to sum them up in one proposition:

**Proposition 2** When $\rho A_t < \pi$, the elite shrinks until in a finite time $S'_h < S_h$ $\rho B_t + S'_h < \pi \leq \rho A_t + S'_h$. The equilibrium size of the elite is smaller due to the external constraint.

When $\rho B_t \leq \pi \leq \rho A_t$, the unconstrained result applies.

Finally when $\pi < \rho B_t$, the elite expands until in a finite time $S'_l < S_l$ its size reaches $1 - \bar{z}$, and the wealth distribution converges towards the degenerate distribution $\rho A(\bar{z}) = \rho B(\bar{z})$ with mass $1$.

If $\pi < \rho B_t$ and $\tau(\bar{z}) < 1 - (1 - c)(1 - T^B)$, the external constraint becomes slack before $S'_l$. In all other cases, taxes, distortions and political rents and inequalities are lower due to the external constraint.

Prop. n°2 yields the same two equilibrium situations than Prop. n°1. The external constraint affects the incomes of the elite and of the masses both in the transition and in equilibrium. The income of the masses is higher relative to autarky, thus offering the possibility of inclusive outcomes when the society would have remained polarized in autarky. The aggregate income of the elite is lower, which either forces the elite to downsize or constrains its rent-seeking ability. In all cases, the external constraint accelerates the convergence, and forces an outcome where taxes, distortions, political rents and inequalities are lower.

### 4.6 Inclusiveness spillovers

Prop. n°2 can easily be extended to account for a non-abating constraint. In other words, let me now simply assume $T_t$ is nonincreasing. As previously clarified, this may correspond to an increasingly inclusive competing jurisdiction, or rather to a general improvement of the institutions in countries with already low costs of doing business. This interpretation provides the first important result of the paper.

**Proposition 3** If the political process becomes more inclusive in a competing jurisdiction, the elite expands iff $\pi < \rho B_t$, with $B_t = B(z_t, T_t) \geq B(z_t)$. It shrinks iff $\pi > \rho A_t$, with $A_t = A(z_t, T_t) \leq A(z_t)$.
Prop. n°3 comes as a corollary of Prop. n°2. Relative to autarky, the tax competition of a inclusive polity abroad results into lower domestic taxes, distortions, political rents and inequalities, and even a faster political convergence. The elite may have to downsize: the range of parameters $\pi$ above which the elite is forced to deplete expands. It may also be forced to become more inclusive: the range of parameters $\pi$ under which it converges towards inclusiveness also expands. To summarize, the external constraint means that increasing political inclusiveness in one country may spillover into increasing inclusiveness in another or, more generally, that increased mobility of a factor of production increases its weight in the policy process. Fig. n°7 illustrates these results.

![Figure 7: Political outcomes in an externally constrained country](image)

To conclude this section, strengthening the external constraint is shown to benefit the inclusiveness of the political process. There are two channels through which this may happen. First, competing jurisdictions may become themselves more inclusive. Second, one may directly affect the costs $c$ of investing abroad. So far, $c$ has been assumed to be exogenous. Let me consider the incentives of the various agents to increase or to decrease this cost. In country $A$, the answer is straightforward: local masses would seek to lower $c$, to increase their own mobility, and local elites to increase it, inasmuch as is in their control. The elite of a constrained country also have an interest in alleviating the external constraint, which may imply helping increase the extractive capacity of the other elite, through an increase in $c$.

Due to its assumptions, the model does not account for any other form of intervention, neither active promotion of inclusiveness by Western liberal democracies, nor social activism in favor of democratization processes abroad. In reality, any number of foreigners may want to team up with local masses to promote inclusiveness. Here, for tractability purposes, investment in the formal sector goes in full to one country; in a more realistic model with simultaneous investment in the domestic and in the foreign formal sectors, investors from abroad will indeed team up with local masses, whether they come from the masses or from the elite abroad. Furthermore, foreigners may also be pursuing geopolitical or moral goals which go beyond the scope of this paper. In short, mobility benefits local masses, foreign investors and migrants, and may even benefit the elite of unconstrained
partner countries (countries with low costs of doing business, eg. liberal democracies). On the contrary, it hurts local elite, and the elite of any country whose fiscal policy is being constrained as a result of this mobility.

5 Captive masses

In the former setup, individuals from the masses and from the elite alike have the ability to emigrate / invest abroad. Under such an assumption, Prop. no 3 establishes that inclusiveness may spillover into a partner country. But mobility may not always extend to the whole population. Now, only the elite can allocate their asset abroad. Such a setup should not be interpreted too literally. There is no reason why there should be an exact coincidence in a given society between being able to extract a rent and being internationally mobile. Arguably, though, the former assumption of universal international mobility, is just another polar situation.

In practice, Rodrik (1997) argued that the international mobility of individuals seems to differentiate individuals according to their professional activity, favoring owners of capital, highly skilled or specific workers, over unskilled, semi-skilled and most middle managers. The degree to which the former have a disproportionate influence over the fiscal policy is key in deciding which assumption – universal mobility or mobility restricted to the elite – is more relevant.

The timeline of the game remains identical. Since the masses never allocated their asset abroad in equilibrium, their program remains the same here: their asset supply can be written $l_t = l(\tau_t) = 1 - (\phi' - 1)(1 - \tau_t)$. Their consumption and bequest functions also remain the same.

Contrary to the previous setup where no actual exchange of assets took place, elite will now sometimes allocate their asset abroad. If $\tau_t \leq 1 - (1 - c)(1 - T_t^B)$, elite too allocate $l_t = l(\tau_t)$ in the formal sector of their own economy. If on the other $\tau_t > 1 - (1 - c)(1 - T_t^B)$, then they allocate $l_t = l(1 - (1 - c)(1 - T_t^B))$ to the other country’s formal sector. If there is not actual asset exchange in equilibrium, the elite’s program remains the same. They then set $\tau_t = \tau(z_t)$ (provided $\tau(z_t) \leq 1 - (1 - c)(1 - T_t^B)$).

5.1 Patrimonial elite

Let me first consider a small country $A$ aside a big country $B$ (also named “abroad”). The elite of $A$ can allocate their asset abroad at no cost ($c = 0$), while the masses are captive (this assumption may seem extreme, but Wong, 2008, derives it as the result of an endogenous policy decision p. 31). Meanwhile, for now, assume they cannot hope to attract any asset from abroad. For instance, the elite may not be able to commit to upholding property rights for foreign investors (Dharmapala
and Hines Jr., 2009). In this paper, patrimonial elite are defined as elite unable to implement good national institutions, and who stash their wealth abroad. Typically, patrimonial elite tend to invest their wealth in liberal democracies, often via tax havens (OECD, 2014, p. 86). Tax havens have two advantages: they generate low costs of doing business, and their secrecy contributes to ensuring the safety of their investment. The program of patrimonial elite can then be written:

$$\max_{\tau_t} (1 - \mathcal{T}_t^B) l(\mathcal{T}_t^B) + \phi(1 - l(\mathcal{T}_t^B)) + \frac{\tau_t z_t l(\tau_t)}{1 - z_t}$$

The elite would then set the tax rate $\tau_t$ so as to maximize rent extraction from their population, at a level $\tau_t = \bar{\tau} > \tau(z_t)$ higher than when they also bore the tax burden themselves. That level does not depend on the size of the elite anymore.

Meanwhile, if $n \gg 1$ is the relative size of “abroad”, the elite in $B$ would set $\mathcal{T}_t^B = \mathcal{T} (z_t^B, 1 - z_t) \approx \tau(z_t^B)$. Elites from $A$ who allocate assets abroad make little or no difference on the policies of $B$: in line with Bucovetsky (1991); Wilson (1991), the larger jurisdiction is less reactive to tax competition than the smaller one.

The elite compare $A(z_t^A)$ when they allocate their own asset domestically with $B(z_t^B) + \frac{z_t^A \tau_l(\bar{\tau})}{1 - z_t^A}$ when they allocate it abroad. For every $z_t^B$, let me define $\theta(z_t^B)$ the subset of $[0, 1]$ such that if $z_t^A \in \theta(z_t^B)$, then the elite would allocate their asset abroad:

$$z_t^A \in \theta(z_t^B) \iff A(z_t^A) < B(z_t^B) + \frac{z_t^A \tau_l(\bar{\tau})}{1 - z_t^A}.$$  \hfill (8)

$\theta$ defines a correspondence from $[0, 1]$ into the partially ordered set of open subsets of $[0, 1]$, with two properties:

**Proposition 4** $\forall z < 1, 1 \in \theta(z)$ and $\theta$ is nonincreasing.

Prop. n°4 fully describes the range of parameters in which the elite in $A$ become patrimonial. First, narrow enough elite ($z_t^A \approx 1$) always have an incentive to stash their wealth abroad and increase rent extraction at home. Second, the rent lost to the elite abroad is smaller for lower $z_t^B$, so patrimonial elite are more likely to be willing to expatriate their assets. Without any more assumptions on $l$ and $\tau$, the description of $\theta$ stops here. I would need further assumptions to show that the frontier of $\theta$ is monotonic, for instance. But this is unnecessary at this point. Let me turn to patrimonial elite dynamics

**Proposition 5** A patrimonial elite expands iff $\pi < \rho B_t$, with $B_t = B(1) < B(z_t^A)$. It shrinks iff $\pi > \rho A_t$, with $A_t = B(z_t^B) + \frac{z_t^A \tau_l(\bar{\tau})}{1 - z_t^A} > A(z_t^A)$.  

25
Prop. n°5 highlights the importance of the mobility of the factors of production for political outcomes. Patrimonial elite maximize rent extraction at home, and thus depress the economic income of the masses. In that context, an inclusive outcome is made very unlikely. Only for the lowest values of $\pi$ can we expect a convergence towards an inclusive situation. When masses are mobile, rent extraction is constrained. Conversely, when masses are captive, taxes, distortions and political rents are higher than if economy was closed, as well as the income of the elite. In that context, a polarized situation may sustain a wider elite (it is therefore unclear how inequalities are affected). To summarize, outcomes when masses are mobile or captive are reversed, as illustrated on Fig. n°8.

\[
\begin{align*}
\text{inclusiveness} & \quad \text{distortions} & \quad \text{elite} & \quad \pi \\
\rho B(z_t^A) & \quad \rho A(z_t^A) & \quad \rho B(1) & \quad \rho \left( B(z_t^B) + \frac{z_t^A \tau_l(t)}{1-z_t^A} \right)
\end{align*}
\]

Figure 8: Political outcomes in a country with a patrimonial elite

Let me now reintroduce a small cost $c > 0$ that the patrimonial elite would lose on their investment abroad. $\theta$ would then have to be written as a correspondence of two variables, nonincreasing in the first variable $z_t^B$, and decreasing in the second variable $c$ until it reaches $\emptyset$. In other words, the elite may be increasingly discouraged to allocate their asset abroad if the cost of doing so increases. This may in turn open the possibility of a more inclusive polity, characterized by lower taxes, distortions, political rents and inequalities. Obviously, local masses would seek to increase $c$, and local elites to decrease it, inasmuch as is in their control. Indeed, whenever the “ill-gotten assets” of patrimonial elite are pursued, it is often at the initiative of non-governmental organizations from the South. Arguably, such actions are raising $c$ and hurting patrimonial elite around the world. Additionally, this model confirms that they may contribute to promoting efficient policies, and even facilitating a change of regime in such countries.

5.2 Supporting patrimonial elites

When masses were assumed to be mobile, due to several simplifications, the model displayed no actual international movement of assets. Patrimonial elite, however, do transfer their assets to more inclusive polities. With no cross-border investments, the incentives of the groups abroad, small as they may be, were shown to be aligned with those of the local masses. Cross-border flows now create
the opportunity for stronger and possibly opposite incentives for some groups in recipient countries to intervene.

Let me consider the big recipient country $B$. The elite there implements a tax rate $T_t^B = T(z_t^B, \frac{1-z_t^A}{n})$, which decreases with $n$. The inflow of the patrimonial elite’s assets increases the relative importance of the extraction motive in the second order. In other words, the big countries are not immune to the existence of the patrimonial regimes: patrimonial inflows might actually favor a polarized outcome over an inclusive one in the bigger jurisdiction.

**Proposition 6** With patrimonial inflows, the elite (in $B$) expands iff $\pi^B < \rho B_t$, with $B_t = (1-T_t^B)l(T_t^B) + \phi(1-l(T_t^B)) < B(z_t^B)$. It shrinks iff $\pi^B > \rho A_t$, with $A_t = B_t + (1+\frac{1-z_t^A}{n}) \frac{T_t^B l(T_t^B)}{1-z_t^B} > A(z_t^B)$.

![Diagram](image)

**Figure 9:** Political outcomes in a patrimonial-friendly country

Fig. n°9 illustrates the results of Prop. n°6. Unlike when masses were mobile, the model now predicts conflicting interests among groups in liberal democracies (and in tax havens). The masses in $B$ still team up with the masses in $A$: indeed non-governmental organizations and multilateral institutions from the North do play a key role in the successful cases of ill-gotten asset retrievals. Now, however, the interests of elite from both countries are aligned. As it is, the model already shows that the democratic elite gain from facilitating inflows of these assets.

In fact, pushing the analysis just one step further shows that the model actually underestimates these gains and the extent of the possible collusion between elite. A successful investment abroad generates additional income for the patrimonial elite. This, however, requires a certain degree of cooperation from the elite of the recipient country. The patrimonial elite may therefore be inclined to bribe the other elite, which may actually substantially bolster the conclusions of Prop. n°6. Such bribes can take several forms, gifts made to key political players or party donations, who may then interfere with judicial procedures targeting ill-gotten assets. While formal democratic procedures restrict, or forbid outright, such practices, they may still be difficult to eradicate.
5.3 Tax havens

In a second scenario, the elite of the small country $A$ is now assumed to be in a position to attract assets from the big country $B$ (still “abroad”). Even if $B$’s masses are mobile, previous considerations have showed that $A$’s elite cannot hope to attract their assets. Let me now assume that $B$ has captive masses and mobile elite (whose assets are for now mobile at a cost $c = 0$). For instance, they may own assets of a different nature, or be in a position to enact special tax provisions and to evade taxes outright.

If indeed $A$’s elite manage to attract the assets of $B$’s elite – this paper’s definition of a tax haven –, they provide the latter with the possibility of increasing the tax rate in $B$. In fact, in the framework of the paper, $B$’s elite are in a position to maximize the rents they extract from their masses, eg. by setting a tax rate of $T^B_t = \hat{\tau}$. Meanwhile, the program of the elite of the tax haven can be written:

$$\max_{\tau_t} (1 - \tau_t)l(\tau_t) + \phi(1 - l(\tau_t)) + \frac{\tau_t(1 + n(1 - z^B_t))l(\tau_t)}{1 - z^A_t}$$

s.t. $A(z^B_t) < (1 - \tau_t)l(\tau_t) + \phi(1 - l(\tau_t)) + \frac{z^B_t\hat{\theta}(\hat{\tau})}{1 - z^B_t}$

If $n$ is big enough, the maximand can be simplified to $\tau_t l(\tau_t)$: both the domestic extraction and the efficiency motives are dwarfed by the rents that can be extracted on the assets of the foreign elite. The policy decision is made irrespective of the local political conditions (the model can even account for a tax haven where nobody qualifies as masses). Only if no level of tax rate would attract the foreign assets would the small country not become a tax haven. In other words, by its mere existence, a big country $B$ such that $\exists z, z^B_t \in \theta(z)$ creates the conditions for a tax haven to appear by its side.

Let me discuss the (admittedly strong) assumptions that underlie this expression. First, tax evasion may actually involve high costs $c$, especially in liberal democracies with strong civil societies. Tax evasion is more likely and more profitable when such societal controls are weak. Second, domestic motives play a role in limiting how low the candidate to tax haven status is willing to set the tax rate. Zucman (2013) estimates that one third of foreign liabilities in Swiss banks belong to Swiss nationals, a share which cannot be neglected in the elite’s program. Nevertheless, it seems very likely that the offshore activity of other tax havens, especially the smaller ones, may account for a much bigger share of their activity. Unfortunately, this has not been documented so far, for want of relevant data. Third, even if domestic motives can indeed be neglected, the candidate to tax haven status may not be able to lower the costs of doing business beyond a certain point, in line with the analysis of Dharmapala and Hines Jr. (2009).

Keeping in mind these considerations, the constraint is binding and $\tau_t$ is on the
“right” side of the Laffer-curve (that is, on the left side): \( \tau_t < \bar{\tau} \).

Whenever there exists a \( z \) such that \( z^B_t \in \theta(z) \), the elite vote on

\[
\tau_t = \max\{\tau(z) : z^B_t \in \theta(z)\} = \tau(\max\{z : z^B_t \in \theta(z)\})
\]

(minus epsilon to break the tie). The effect of tax evasion on the political dynamics of the tax haven is ambiguous. The tax policy is “flooded” by foreign motives. The elite may set a higher tax rate to take advantage of the asset flight than they would in a closed economy, which would result into higher distortions and political rents, and a more likely polarized outcome. The shape of \( \theta \), however, makes the converse scenario, where they actually set a lower tax rate, more likely: this would result in less inequalities, less distortions, and possibly a transition to an inclusive political regime. Notice that such a transition illustrates the ambiguity of using political inclusiveness as a proxy for democracy: in a tax haven, inclusiveness may grow, though maybe not transparency, another key ingredient of democracy.

5.4 Tax evasion

Again, the existence of tax havens involves actual movements of assets. Let me therefore examine the resulting interests of the various stakeholders.

Proposition 7 The tax evading elite expands iff \( \pi^B < \rho B \), with \( B_t = B(1) < B(z^B_t) \). It shrinks iff \( \pi^B > A(z^B_t) \).

\[
\begin{align*}
\text{inclusiveness} & \downarrow \quad \text{distortions} \uparrow \\
\rho B(z^B_t) & \quad \rho A(z^B_t) \\
\rho B(1) & \quad \pi^B
\end{align*}
\]

Figure 10: Political outcomes associated with tax evasion

Fig. n°10 illustrates the results of Prop. n°7. Due to tax evasion, taxes, distortions, rents and inequalities increase, which favors a polarized outcome in \( B \). The elite in the tax haven are actually in a position to capture the whole rent surplus, and in the first order \( B \)’s elite derive no benefit from evading their own tax system. A more careful analysis of the model reveals at least two mechanisms

\[\footnote{The proof is by contradiction. Suppose the constraint is not binding. Then \( \tau_t = \bar{\tau} \). The right hand-side of the inequality would then be \( B(1) + \frac{\tau_t^B z_t}{1-\tau_t} < B(1) + \frac{\tau_t^B z_t}{1-\tau_t} \), which by definition is less than \( A(z^B_t) \).} \]
through which B’s elite may keep their share of the surplus (maybe then Fig. n°9 is a better illustration than Fig. n°10). First, arguably, B’s elite may be the group of individuals best positioned to successfully create a tax haven. Theoretically, another group could possibly do so as well; however the elite’s own tax haven is much more beneficial to the elite. In that case, the interests of the elite of A and B are obviously aligned, since they are the same actual individuals. Such a mechanism is consistent with the existence of several non-sovereign tax havens, and with the very close association of the governments of even the most advanced liberal democracies with generally one, and sometimes a few tax havens. Second, even if B’s elite is not in a position to create their own tax haven, there may be an opportunity for the existence of not one, but several tax havens. The ensuing competition for the location of the assets may improve the bargaining position of B’s elite. As a result, in the model, the interests of both elite might in fact coincide in lowering c insasmuch as is in their control, to the detriment of the masses in B, who will try to increase c. The interests of A’s masses (if such a group actually exists) are unclear. If anything, capital flight may give an incentive to lower the level of taxes in the tax haven, and the incentives of the masses are more likely to be aligned with the interests of elite.

Does that mean that the fight against tax evasion is hopeless? No, but this analysis reveals that it is maybe illusory to expect the governments of even the most advanced liberal democracies to credibly threaten tax havens. Under the first mechanism, the tax haven is an essential determinant of their accumulation of wealth, and under the second one, they would favor the emergence of more tax havens, rather than risk reducing their own bargaining position against tax havens by reducing their ranks. The only credible actors in this fight necessarily come from the strong civil societies of liberal democracies, and in particular their judicial systems, inasmuch as they are indeed independent from the executive and legislative branches of the government.

References


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A Proof that the two-stage game of fiscal competition is weak-dominance solvable

The proof proceeds by iterated elimination of weakly dominated strategies, which can yield only one undominated strategy if done correctly. Let me consider the game in normal form with two countries $i$ and $j$, where a strategy for the elite of country $i$ can be written $\{T^i, t^i\}$, where $T^i$ is the tax rate set in period 2 and $t^i$ is a mapping which to any tax rate $T^j$ set by the elite of country $j$ in stage 2 associates a tax rate $t^i(T^j)$ set by the elite of country $i$ in stage 3:

$$t^i : T^j \rightarrow t^i(T^j).$$

For notational convenience, let me write $T^{i*} = T(z^i, n)$ and $T^{j*} = T(z^j, \frac{1}{n})$. Let me consider one process of iterated elimination which yields only the desired strategy.

1. Any strategy $\{T^i, t^i\}$ such that $\exists T^j, t^i(T^j) < \min[1 - (1 - c)(1 - T^j), \tau(z^i)]$ is weakly dominated by the strategy $\{T^i, T^j \mapsto \max\{t^i(T^j), \min[1 - (1 - c)(1 - T^j), \tau(z^j)]\}\}$. Obviously $T^j \mapsto \max\{t^i(T^j), \min[1 - (1 - c)(1 - T^j), \tau(z^j)]\}$ is nondecreasing.

2. Any remaining strategy $\{T^i, t^i\}$ such that $T^i > T^{i*}$ is weakly dominated by the strategy $\{T^{i*}, t^i\}$.

3. Any strategy $\{T^i, t^i\}$ such that $t^i$ is not nondecreasing is weakly dominated by the strategy $\{T^i, T^j \mapsto \max_{t \in [0, T^j]} t^i(t)\}$. Obviously $T^j \mapsto \max_{t \in [0, T^j]} t^i(t)$ is nondecreasing.

4. Any remaining strategy $\{T^i, t^i\}$ such that $t^i(T^{j*}) > 1 - (1 - c)(1 - T^{j*})$ is weakly dominated by the strategy $\{T^i, T^j \mapsto \min\{t^i(T^j), t^i(T^{j*})\}\}$.

5. Any remaining strategy $\{T^i, t^i\}$ such that $T^i < T^{i*}$ is weakly dominated by the strategy $\{T^{i*}, t^i\}$.

6. Any remaining strategy $\{T^{i*}, t^i\}$ such that $\exists T^j, t^i(T^j) > \min[1 - (1 - c)(1 - T^j), \tau(z^j)]$ is weakly dominated by the strategy $\{T^{i*}, T^j \mapsto \min[1 - (1 - c)(1 - T^j), \tau(z^j)]\}$.

The only strategy standing at the end of the iterated elimination process is $\{T^{i*}, T^j \mapsto \min[1 - (1 - c)(1 - T^j), \tau(z^j)]\}$.
B  Extension 1: Public inputs

In the standard setup, I considered the state only as an instrument of predation for the elite. However, the state and the elite have traditionally fulfilled another important function: they also provide public goods essential for economic activity (public inputs). Obvious examples are education, health, transport and communication infrastructure, public institutions and defense. In fact, this second function of providing essential public inputs arguably accounts for a much larger share of the state’s revenue than rent-extraction.

As I show here, in the standard, most general case, fiscal competition should both increase the provision of public inputs and decrease the fiscal pressure: the state should only be forced to become more efficient, from the productive sector’s point of view. Except for that important reinterpretation, public inputs provision is here presented only as an extension of the model, because it does not substantially alter the conclusions of a competition limited to taxes. All previous results extend here.

B.1 The setup

In this section, I extend the model to account for the provision of public inputs. The elite use part of the revenue of taxation to finance public inputs. What remains is the political rent they manage to extract.

Let me follow Ades and Verdier (1996) to account for a positive and equal effect of the provision of public inputs on the productivity of the formal and informal activities. Technology in the formal sector is such that \( lt \) units of labor produce \( h(g_t)l_t \) units of output, and in the informal sector such that \( l_t \) units of labor produce \( h(g_t)\phi(l_t) \) units of output. \( g_t \) is the per capita amount of public inputs provided by the state. The marginal return of public inputs provision is assumed to be positive and increasing, so \( h' > 0, h'' < 0 \). For there to be any public input provision, the marginal benefit of the first unit of public input must be higher than the cost of public funds: \( h'(0) > 1 \). The structure of the game is the same as the first game of tax competition with no public input provision, except that in stage 2, the elite can now choose both the tax rate and the way in which the resulting tax revenue is allocated between redistribution (to itself) and the provision of public inputs: \( g_t \) if it keeps its national asset only.

Now that the informal sector can be directly affected by the elite’s policy, eg. public input provision, I need to actually make an assumption on the location of an individual’s informal asset. For simplicity, let me assume that any individual can only have his activities, both formal and informal, in the same country. In other words, an individual cannot benefit from the high provision of public inputs in the informal sector of a country and from the low tax rate in the formal sec-
tor of another country. Under this useful assumption, whether the public input affects either or both of the formal and informal sector becomes irrelevant. This assumption, reasonable as it may sound, is not straightforward, and I discuss its implications later.

B.2 Fiscal policy

Solving the game backwards, in that case, the equal effect of public inputs on both domestic sectors ensures that the labor supply still depends only on the effective tax rate (to still be interpreted as the cost of doing business, which fully accures to the elite) $\tau_i$ born by the individual. It can still be defined by $1 - \tau_i = \phi'(1 - l_i)$, and therefore still by $l_i = l(\tau_i)$. With public inputs, the economic income should now be written $Y(g_i, \tau_i) = h(g_i)B(\tau_i)$.

By analogy, the external environment can be characterized by a tax rate $T_t$, and by a provision $G_t$ of public inputs. As in the case without public input, the masses never allocate their asset abroad in equilibrium: indeed, suppose the elite decided to allow the asset flight. They would derive an income $Y_t = Y(G_t, 1 - (1 - c)(1 - T_t))$, and since there is no domestic activity to tax, no economic rent. By setting for instance $\tau_t = T_t$, however, they ensure that they would be able to match the other country’s provision of public input; and if they do, they would derive an economic income $Y(G_t, T_t) > Y_t$, plus a nonnegative political rent from taxing the domestic asset. Therefore the elite is always better off making sure it retains the national assets on the domestic territory.

In stage 2, the the program of the elite can therefore be written:

$$\max_{\tau_t, g_t} Y(g_t, \tau_t) + \frac{\tau_t h(g_t) l(\tau_t) - g_t}{1 - z_t}$$

s.t. \begin{align*}
\tau_t h(g_t) l(\tau_t) &\geq g_t \geq 0 \quad \text{budget constraint} \\
Y(g_t, \tau_t) &\geq Y_t \quad \text{no asset export}
\end{align*}

Writing $\lambda_t$ the Lagrange multiplier for the budget constraint in stage 3 and $\mu_t$ the Lagrangian multiplier for the no asset export constraint, this program yields the following first order conditions

$$\begin{cases}
-(1 + \mu_t)l + (\tau_t l' + l) \left( \frac{1}{1 - z_t} + \lambda_t \right) = 0 \\
(1 + \mu_t)h' B + (h' \tau_l l - 1) \left( \frac{1}{1 - z_t} + \lambda_t \right) = 0
\end{cases}$$

and exclusion conditions $\lambda_t > 0$ if $\tau_t h l = g_t$, $\lambda_t = 0$ if $\tau_t h l = g_t$, $\mu_t > 0$ if $Y(g_t, \tau_t) = Y_t$ and $\mu_t = 0$ if $Y(g_t, \tau_t) > Y_t$. In equilibrium, political rents will never be less than $\pi$, which implies that $\lambda_t = 0$. As without public inputs, I will first consider the unconstrained fiscal policy ($\mu_t = 0$), and then the impact of the constraint ($\mu_t > 0$).
B.3 Unconstrained fiscal policy

When a country is unconstrained by the fiscal competition of another, \( \mu_t = 0 \) too. Under condition (C1), the elite sets \( \tau_t = \tau(z_t) \) in stage 2, the same as without public inputs. Notice that this tax rate is determined independently from the level of public input provision. This is good news, as it ensures the model is robust to changing the specification to one where public input provision can only happen once the taxes have been raised. Also, the tax rate is still decreasing in the size of the elite (increasing in \( z_t \)).

The provision \( g_t \) of the public input results from the optimal allocation of tax revenue between public inputs and transfers to the elite itself. At the margin, public input provision affects positively the elite’s income through two channels: through its increased own economic income, and through a wider tax base. Since public input provision comes at a marginal cost of \( \frac{1}{1-z_t} \) in terms of transfers, the elite balances the costs and benefits by providing the optimal level of public inputs \( g_t = g(z_t) \) such as \( (1-z_t)B(z_t) + \tau(z_t)l(\tau(z_t))h' = 1 \). \( g \) is a decreasing function of \( z_t \). In other words, as the size of the elite increases, the amount of state revenue allocated to the provision of public inputs increases. The intuition is simple: as the elite broadens, transfers have to be shared among more elite members, and the return to allocating tax revenue to transfers decreases.

The political rent can therefore be written \( R_t = R(z_t) = \frac{\tau(z_t)h'(g(z_t))l(\tau(z_t))g(z_t)}{1-z_t} \), with \( R \) an increasing, continuous function of \( z_t \), \( R(0) = 0 \) and \( R(1) = \infty \). In stage 1, the same conditions determine entry into the elite: first, \( b_t \geq \pi \), and second \( R_t \geq \pi \). There exists a unique \( z \) such that \( R(z) = \pi \).

A quick word on the composition of the elite. The liquidity condition is the same here as it was without any public input provision; the profitability condition, on the other hand, is much more stringent, and also much more realistic. Elite dynamics now explicitly focus on small elites, though all is conceptually equivalent. The dynamics of wealth accumulation, and therefore of elite dynamics, are essentially the same as without public inputs, as described by Eqs. n°6 and 7, with incomes now defined by

\[
\begin{align*}
A_t &= A(z_t) = Y(g(z_t), \tau(z_t)) + R(z_t) \\
B_t &= B(z_t) = Y(g(z_t), \tau(z_t)).
\end{align*}
\]

Public inputs are only provided if \( h'(0) > 1 \), in which case the simple existence of the public inputs raises the income of the masses, and reduces the political rent extracted by the elite. As could be expected, inequalities are unequivocally lower than in the case without public inputs. Yet the nature of the political dynamics is not modified by the provision of public inputs: as without public inputs, \( A \) and \( B \) are respectively increasing and decreasing in \( z_t \).

When \( \pi \) is high, eg. when \( \rho A_t < \pi \), the elite shrinks until it stabilizes in a
finite time. The tax rate increases, and as a novelty, the provision of public input diminishes. Political rents and economic distortions still increase. Once again, the definition of inequalities would need to be further specified in order to provide a prediction, but this is not central to this analysis. After the size of the elite stabilizes, taxes and public input provision remain constant.

When \( \pi \) is intermediate, e.g., when \( \rho_B \leq \pi \leq \rho_A \), the elite remains stable at its initial size, with no entry or exit. The tax rate, public input provision, political rents, distortions and inequalities remain constant.

Finally, when \( \pi \) is low, e.g., when \( \pi < \rho_B \), the size of the elite increases as fewer individuals are liquidity constrained. As more people get involved in the fiscal decision making, taxes, distortions and political rents fall, as well as inequalities. Meanwhile, provision of the public input increases: the state becomes more productive and less redistributive. Because of a smaller tax burden and a better allocation of tax revenue to market activities, output increases until the profitability constraint becomes binding (which happens faster than without public inputs, since \( \bar{\tau} \) is higher), and the output stabilizes.

To summarize, allowing the state to provide public inputs confirms the findings of Prop. n°1. The political and economic nexus allocates resources in a more efficient way as there are less political rents, and a faster spread of political access. When taking into account that the elite can provide public inputs, a reduction in the cost of political participation \( \pi \) has two effects. First, it reduces allocative distortions by lowering the tax rate imposed on manufacturing activities. Second, it improves the allocation of tax revenue, by increasing the share devoted to the provision of the productive public input.

### B.4 The external constraint

In equilibrium, the elite would always manage to retain the assets of the masses by providing them with an income \( Y(g_t, \tau_t) \geq \mathcal{Y} \). Following the same line of arguments as without public inputs, in a two-country setup, I can provide a model of \( \mathcal{T}_t^B \) and \( \mathcal{G}_t^B \) where they are the unique strategy to yield an extensive-form trembling hand perfect equilibrium, and the unique strategy resulting from a process of iterated elimination of weakly dominated strategies: the program of the foreign elite can be written

\[
\max_{\mathcal{T}_t^B, \mathcal{G}_t^B} \left[ Y(\mathcal{G}_t^B, \mathcal{T}_t^B) + \frac{\mathcal{T}_t^B h(\mathcal{G}_t^B) \left( 1 \left( \mathcal{T}_t^B \right) + nl \left( 1 - (1 - c) \left( 1 - \mathcal{T}_t^B \right) \right) \right) - (1 + n) \mathcal{G}_t^B}{1 - z_t^B} \right] \\
\text{s.t. } \mathcal{T}_t^B h(\mathcal{G}_t^B) \left( 1 \left( \mathcal{T}_t^B \right) + nl \left( 1 - (1 - c) \left( 1 - \mathcal{T}_t^B \right) \right) \right) \geq (1 + n) \mathcal{G}_t^B.
\]

The constraint is not binding. The elite therefore vote on \( \mathcal{T}_t^B = T(z_t^B, \frac{1}{n}) \), the same as without public inputs. Notice that this tax rate is determined indepen-
dently from the level of public input provision. This is good news, as it ensures the model is robust to changing the specification to one where public input provision can only happen once the taxes have been raised. Also, the tax rate is still decreasing in the size of the elite (increasing in $z^B$). The elite also vote on $G_t^B = G(z^B_t, \frac{1}{n})$ such that $(1 - z^B_t)B(T^B_t) + T^B_t(B(l(T^B_t) + nl(1 - (1 - c)(1 - T^B_t))))h' = 1 + n$. The first partial derivative of $G$ is negative. In other words, as the size of the elite increases, the amount of state revenue the elite is willing to allocate to the provision of public inputs increases.

Let $Y^B_t = Y(z^B_t, 1, n) = Y(G(z^B_t, 1, n), 1 - (1 - c)(1 - T(z^B_t, 1, n)))$ be the economic income an individual can derive from allocating his asset abroad. The fiscal constraint is effectively binding when $Y^B_t > Y(g(z_t), \tau(z_t))$, which also corresponds to $\mu_t > 0$. $G$ is decreasing and $T$ increasing in $z^B_t$, so $Y$ is decreasing in $z^B_t$. In other words, the income offered on an investment abroad is higher if the polity abroad is more inclusive, which we take as a reasonable description of the external constraint on the fiscal policy, and a very straightforward extension of the standard model.

### B.5 Constrained fiscal policy

Let me now consider stage 2, when the fiscal policy is externally constrained. In that case, the program of the elite can be simplified into

$$
\max_{\tau, g_t} h(g_t)\tau_t l(\tau_t) - g_t
$$

s.t. $h(g_t) B(\tau_t) \geq Y^B_t$

where the constraint is now binding, and can be defined as an increasing function in the $(\tau_t, g_t)$-plane. This function moves northwestward when $Y^B_t$ increases.

Once again, this program is compatible with an alternative setting where public input is provided only once the taxes have been raised. The problem yields two first order conditions in $\tau_t$ and $g_t$. Eliminating $\mu_t$ between these two expression can be shown to yield

$$
\frac{1}{h'(g_t)} = \frac{l(\tau_t) + \tau_t l''(\tau_t)}{l(\tau_t)} B(\tau_t) + \tau_t l(\tau_t).
$$

(11)

For a well defined concave problem,\(^7\) the right hand side of this equality is a decreasing function of $\tau_t$, while the left hand side is an increasing function of $g_t$. Therefore the first order condition defines a decreasing function in the $(\tau_t, g_t)$-plane, independent of $Y^B_t$. As a consequence, when the no export constraint is

\(^7\)The derivative of the right hand side has the same sign as $l(\tau_t)l''(\tau_t) + \tau_t l(\tau_t)l'''(\tau_t) - \tau_t l'(\tau_t)^2$. Under (C1), this expression is negative. I am making no further assumption here.
binding and $Y_t^B$ increases, the elite both lowers the level of taxes and expands the provision of public inputs.

**Proposition 8** $\frac{d\tau_t}{dY_t^B} < 0$ and $\frac{dg_t}{dY_t^B} > 0$.

As when the country is fiscally independent, the dynamics of wealth accumulation are essentially the same when taking into account the provision of productive public inputs. Inequalities are unequivocally lower than in the case without public inputs. Props. n°2 and 3 can be immediately extended here. Prop. n°8 characterizes the provision of public inputs during the transition and in equilibrium. When $\pi$ is high, the elite shrinks until it stabilizes in a finite time. Taxes are lower than if the country were independent, and a higher public input provision further depresses the income of the elite, whose depletion is accelerated as a result. Political rents and economic distortions are lowered by the fiscal competition, and the output is higher, thanks to an expanded provision of public inputs.

When $\pi$ is intermediate, the elite remains stable at its initial size, with no entry or exit. As previously, taxes, distortions and political rents are lower than if the country were fiscally independent, and public input provision is higher. Finally, when $\pi$ is low, applies. The size of the elite increases and fewer individuals are liquidity constrained. Taxes, distortions, political rents and inequalities fall, while public input provision increases.

Similarly, the intuitions of Props. n°4, 5, 6 and 7 survive the introduction of public inputs.

Prop. n°8 therefore offers a novel insight, accounting for a simultaneous decrease of the costs of doing business and increase in the provision of public inputs in the face of an external constraint. Under fiscal competition, public input provision and the tax policy are complementary tools for the rent-seeking elite who wish to avoid an asset flight, quite intuitively: if the tax rate is interpreted as accounting for the costs of doing business, the public input can after all be considered as a negative cost. The state is more productive and less redistributive (towards the elite) than without the external constraint. Under the budget constraint, without rent extraction, a lower tax revenue would mechanically translate into less public expenditure. Taking into account rent extraction, however, shows that the fiscal competition impacts the rents extracted, not the provision of public inputs.

This proves that in the main model, “taxes” were rents extracted, strictly speaking, inefficiencies associated with distortions of the productive sectors, the costs of doing business with no matching institutions or public inputs.
C Extension 2: Mineral rents

Suppose that the country contains mineral resources, which can possibly provide a period income of $W$. Point-source resources are controlled by the state, and in the absence of a mechanism of violent overthrow of the elite, are uncontested by the masses. The asset supply function is independent from the presence of minerals. Logically, income derived from mineral extraction is not taxed (or if it is, it is strictly for show, since the beneficiaries of the tax proceeds coincide with those who bear the burden of the tax). Therefore, the tax policy of the elite remains unchanged, as well as the income of the masses, whether $B(z)$, $B(z,T)$ or $B(1)$, in the corresponding situations.

The income of the elite, however, is increased relative to each of these situations. This additional mineral rent is shared among members of the elite, who thus derive an additional individual income of $\frac{W}{1-\gamma}$ from mineral extraction. The equilibrium dynamics are the same, with one exception: if $W$ is big enough, eg. $W \geq \pi$, the profitability constraint is never binding. The logic of Props. 1 and 2 is maintained throughout, at least when $\pi$ is not too low. When $\pi$ is low, if $W \geq \pi$, the elite expands until its size reaches 1, with all members of the society sharing the benefits of the mineral rent.

Keeping the notation $A_t$ and $B_t$ for the incomes of the elite and of the masses without the mineral rents, the following proposition ensues:

**Proposition 9** The elite expands iff $\pi < \rho B_t$, and taxes shrink to 0 in a finite time iff additionally $W \geq \pi$. It shrinks iff $\pi > \rho A_t + \frac{W}{1-\gamma}$.

In any of the cases under consideration in this paper, the presence of mineral rents may allow a wider elite to maintain itself in control. While in the current period they do not affect taxes, dynamically and in equilibrium they may therefore favor lower taxes and distortions imposed on the productive sector. They unequivocally increase the level of inequalities, in the dynamics and in equilibrium (except when $\pi < \rho B_t$: in this case, the society eventually reaches a state of perfect equality, as without rents). Mineral rents, however, do not change the outcome if the political process is to become inclusive ($\pi < \rho B_t$) or to remain polarized ($\rho B_t \leq \pi$).

This simple framework is maybe too simple, and cannot provide further insights. Any further discussions of the role of mineral rents in tax evasion, for instance, would require assumptions with an important risk that they would be ad hoc, or would lead to a much more complex model than used in this paper.